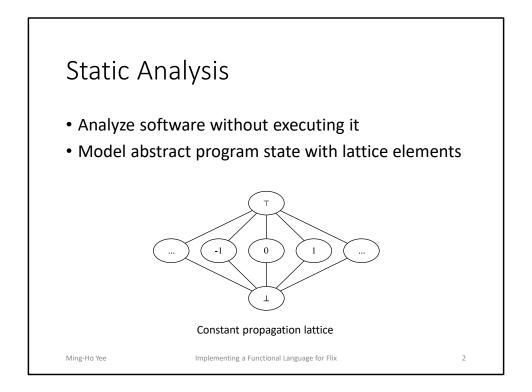
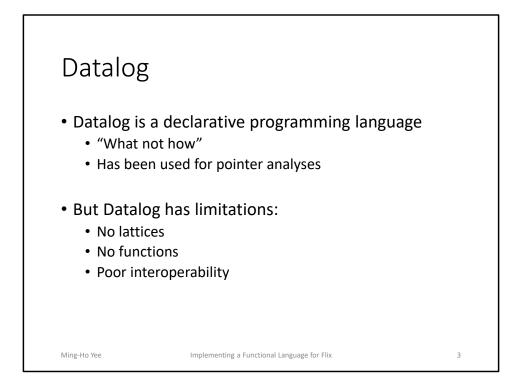


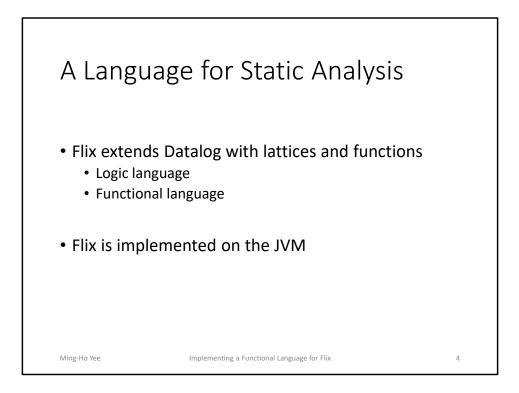
- Today I'm going to be talking about what I worked on for my thesis.
- Flix is a project I've been working on with Ondřej and Magnus.
 - We've also had two undergraduates who have worked on Flix (Billy and Luqman).
 - My focus has been the functional language back-end.



- Static analysis: technique for analyzing software without executing it.
 - Applications: compiler optimizations, code refactoring, bug finding.
- A static analysis typically models abstract program state as elements of a lattice.
 - Ordering represents precision, lower = more precise.
 - Example: constant propagation lattice.



- One approach to implementing static analyses is to use Datalog.
 - Datalog is a declarative language: what not how.
 - Specify the constraints of the analysis, and a Datalog solver finds the solution.
 - Much easier to understand and maintain than using Java or C++
 - Many researchers have used Datalog to implement pointer analyses
- But Datalog has some limitations:
 - No user-defined lattices
 - No functions
 - Poor interoperability
- Some analyses cannot be expressed in Datalog.
- Using Datalog with existing tools and front-ends is difficult.



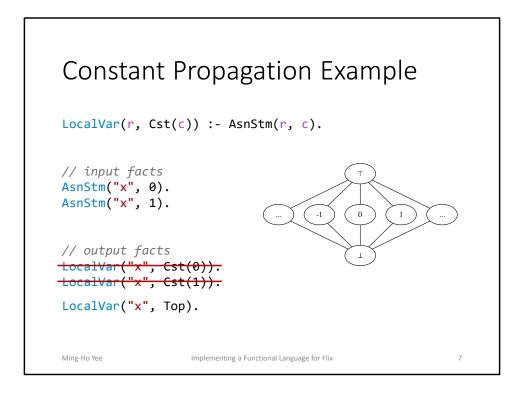
- Flix extends Datalog with user-defined lattices and functions.
 - Specify analysis constraints in the logic language.
 - Based on Datalog and supports user-defined lattices.
 - Express user-defined functions in the functional language.
 - Pure and strict, supports let-bindings, first-class functions, pattern matching.
 - Supports the Java integer types, including BigInteger. Also supports tags and tuples.
- Flix is implemented on the JVM.
 - Interoperability with JVM languages.
 - Call Flix from a JVM language, call JVM code from Flix.

Constant Propagation in Flix (1/2)enum Constant { case Top, case Cst(Int), case Bot } def leq(e1: Constant, e2: Constant): Bool = match (e1, e2) with { case (Bot, _) => true case (Cst(n1), Cst(n2)) => n1 == n2 case (_, Top) => true case _ => false } def lub(e1: Constant, e2: Constant): Constant = ... def glb(e1: Constant, e2: Constant): Constant = ... def sum(e1: Constant, e2: Constant): Constant = ... Implementing a Functional Language for Flix Ming-Ho Yee 5

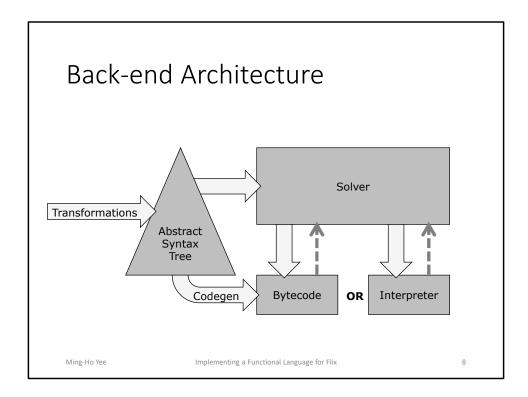
- Here is what constant propagation looks like in Flix.
 - Some details are omitted for brevity.
- First, look at the functional code.
- We define a tagged union, Constant.
 - Represents elements of the constant propagation lattice.
- We define the three lattice operations:
 - leq, lub, glb
 - leq is an example of pattern matching.
- sum is a separate function, more on that later.

// Constant Propagation in Flix (2/2) // analysis inputs Prime Prim

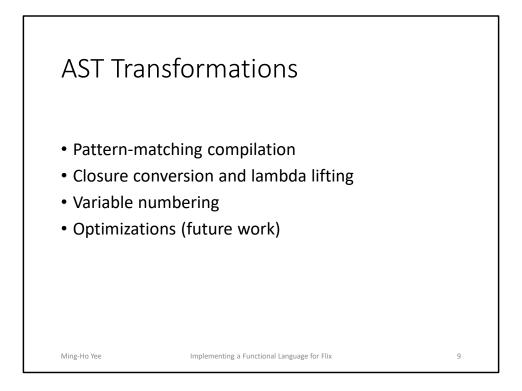
- Now for the logic code.
- We define two relations, AsnStm and AddStm, as inputs.
 - Variable r is assigned the integer c
 - Variable r is the result of x + y
- We define the LocalVar lattice, which is the output the analysis computes.
 - Variable k has value v.
 - LocalVar is a map lattice, where k is the key and v is the value.
- First rule: if we assign c to r, then we know the variable r has value c.
- Second rule: if we're adding two variables and know their values, we can compute the value of the result, using the sum function.



- Here's a small example of how Flix handles lattices.
 - We'll look at the first rule, and two input facts.
- Evaluating the rule, we infer that the local variable "x" has value 0 and 1.
 - But LocalVar is a lattice. We have two values for the same key.
 - We have to compress the values, using the lub operation.
 - This gives us Top.
- In the static analysis, we don't know the exact value for "x".
 - So we approximate by saying the value is Top.



- After several phases, the front-end produces a TypedAst.
- The TypedAst goes through several transformations, becoming a SimplifiedAst and then an ExecutableAst.
 - Compiles higher-level constructs like pattern matching into lower-level primitives.
 - We'll discuss pattern matching and lambda functions.
- Execution starts in the solver, which evaluates rules of the logic language.
 - During this process, the solver may need to evaluate functional code.
 - i.e. lattice operation (lub), or an explicit function call (sum)
 - After evaluating the function, the result is returned to the solver.
- Two implementations of the functional language:
 - Interpreter was original, and is for debugging and prototyping.
 - JVM bytecode generator is newer, and for performance.
- This presentation will cove the code generator.

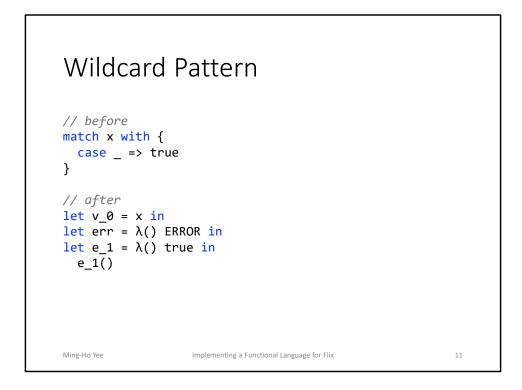


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- Before code generation, a number of AST transformations are required.
 - The interpreter doesn't really need any of this.
 - But to keep things consistent, the interpreter and code generator consume the same AST
- First is to compile pattern matching from a high-level representation into lower-level primitives.
- Then we need to do a few transformations to implement lambda functions.
- Variable numbering is self-explanatory.
 - Numbers are needed so the code generator can emit load/store instructions.
- Finally, AST transformations go here.
 - Currently none, but they could be constant propagation, copy propagation, dead code elimination.
- Today I'll discuss pattern-matching compilation and closure conversion.

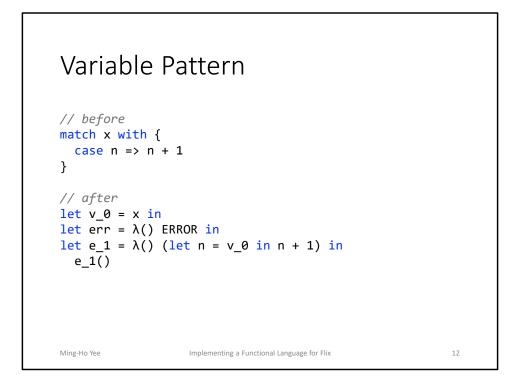
Compiling Pattern Matching

```
// before
match x with {
    case PAT1 => EXP1
    case PAT2 => EXP2
    case _ => ERROR // implicit default case
}
// after
let v_0 = x in
let err = \lambda() ERROR in
let e_2 = \lambda() if (PAT2 succeeds) EXP2 else err() in
let e_1 = \lambda() if (PAT1 succeeds) EXP1 else e_2() in
    e_1()
```

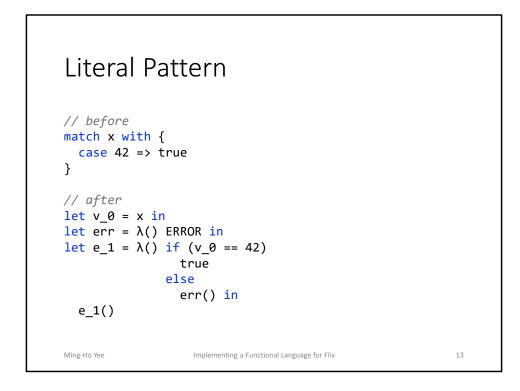
- First transformation to discuss is pattern-matching compilation.
- This is all pseudocode.
- In the pattern match, the expression x is compared against the patterns.
 - If it matches, then the corresponding expression is evaluated.
 - If nothing matches, the expression throws an error.
- It's straightforward to implement this in an interpreter, but not so for a code generator.
 - We want to transform to something simple. Let-expressions, if-expressions, functions, and other primitives.
- Two main steps: create the hierarchy of let-expressions, then transform the patterns.
 - Need to generate fresh names for the variable being matched (so we don't evaluate it multiple times), each case, and the error case.
 - Construct the let-expressions inside-out, so a case can refer to the next one.
 - Finally, construct a call to the function representing the first case.



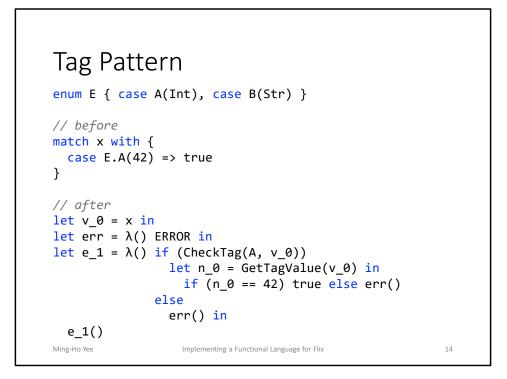
- There are five types of patterns, and each needs to be handled specifically.
- A wildcard pattern matches everything and also succeeds.
- So the transformation is simply the body of the case.



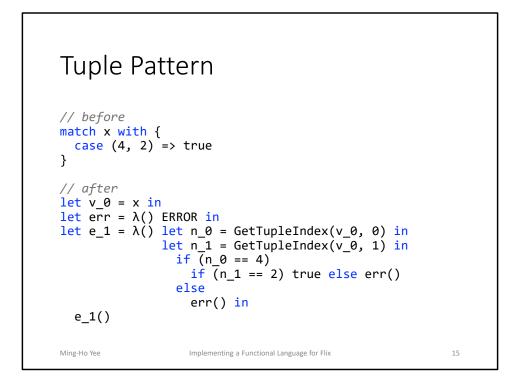
- A variable pattern always succeeds, but it binds the matched value to a name.
 - This is typically used in subpatterns to extract value from tags and tuples.
- The transformation is a let-expression in the body of the case.



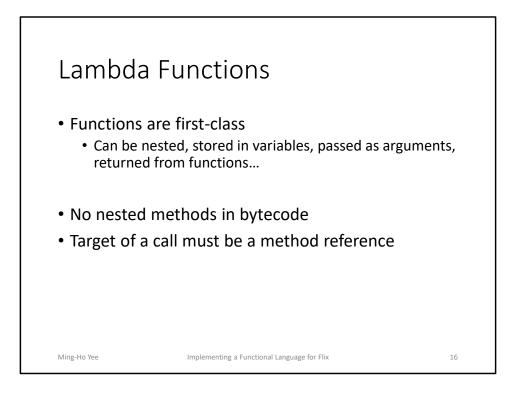
- A literal pattern succeeds if the value equals the literal in the pattern.
 - This pattern checks if x == 42.
- This translates to an if-expression and an equality check.
 - The true branch is the body of the case.
 - The false branch is a call to the next case.



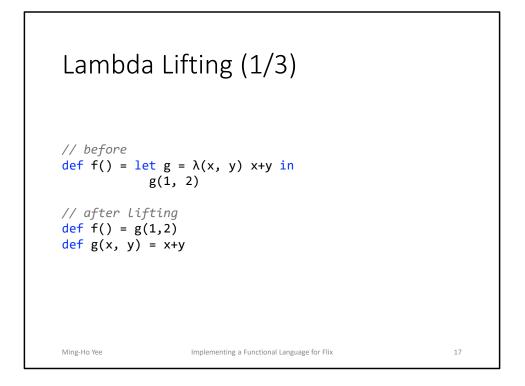
- A tag pattern succeeds if the enum and tag names match, and the subpattern also matches.
 - This pattern checks that x is the tag E.A, and its inner value == 42.
- In this example, E is a tagged union with tags A and B.
 - E is the enum name, A and B are the tag names.
- The pattern match uses the CheckTag primitive.
 - Note that the type checker guarantees that v_0 is a member of the E tagged union.
 - If the check succeeds, then we bind the inner tag value to a fresh name, using a let-expression and the primitive GetTagValue.
 - Then we have the transformed subpattern.
 - If the subpattern or the CheckTag fail, then we evaluate the error case.



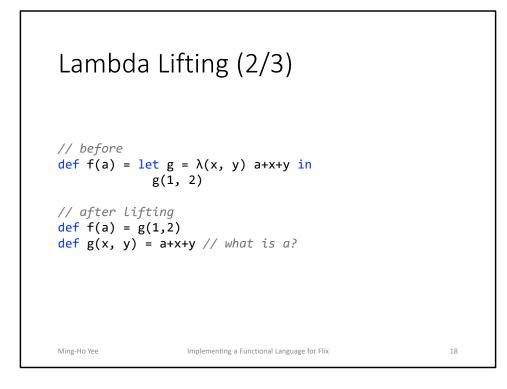
- A tuple pattern contains multiple subpatterns, each corresponding to a tuple element.
 - The type checker guarantees the type and arity of x matches the patterns.
- The transformed pattern extracts the tuple elements, using GetTupleIndex, and binds them to fresh names.
 - Then each subpattern is translated.
 - If everything succeeds, the body of the case is evaluated.
 - If anything fails, the next case is evaluated.



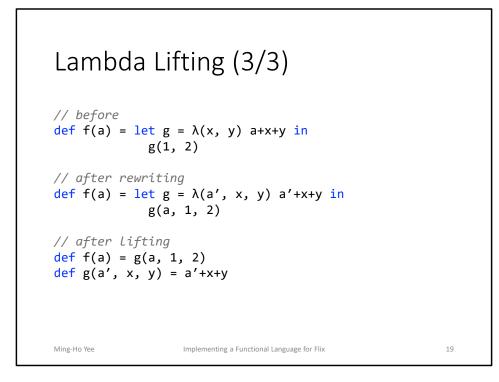
- In Flix, functions are first-class.
 - You can nest function definitions, store a function in a variable, pass it as an argument, and return from a function.
- This does not hold for bytecode.
 - All methods must be defined at the top-level. No nesting.
 - The target of a method call must be a method reference.
 - Cannot be an arbitrary expression that evaluates to a function.



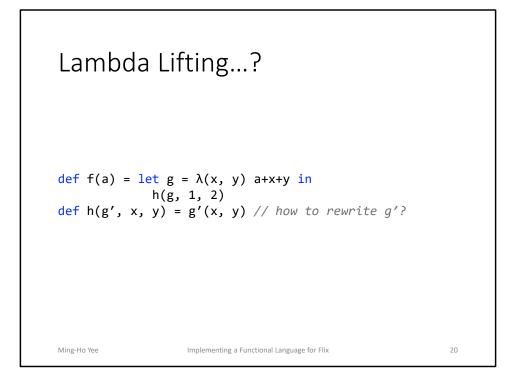
- We solve the first problem (nested functions) with lambda lifting.
 - Self-explanatory name: we lift a nested lambda definition to the top level.
- In this example, within the definition of f, we bind a function to g, and then call g.
- The transformation simply lifts the inner definition.
 - g now refers to a function and not a local variable.



- But what about free variables?
- If we naïvely lift, then we have a definition with an unbound variable.
- So lambda lifting must account for free variables.



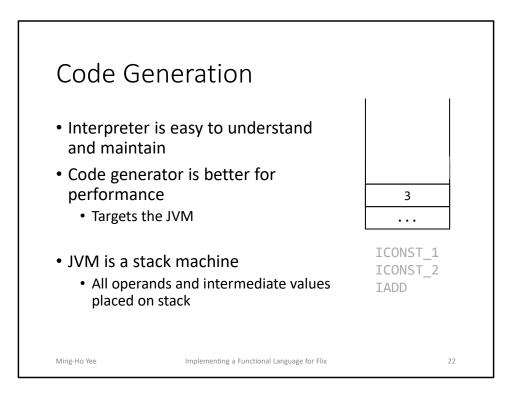
- We rewrite the function to pass the free variable as an extra parameter.
 - Our convention is to prepend the free variables to the parameter list.
 - Note that the call site must also be rewritten.
- Now we can safely lift the lambda.



- Rewriting all the call sites is pretty annoying.
- But it gets worse: what if you can't rewrite the call site?
 - What if we pass a function as an argument?
- In this example, g needs to be rewritten to take an extra parameter.
 - But how do we know that we need to rewrite g'?
 - What if some other function passes in a different g that doesn't need to be rewritten?
- Real problem: variables are bound at different times.
 - a is bound when the lambda is created.
 - x and y are bound when the lambda is called.
- Solution: use closures.
 - Store the data (variables that are bound when closure is created)
 - Store the code (reference to function)

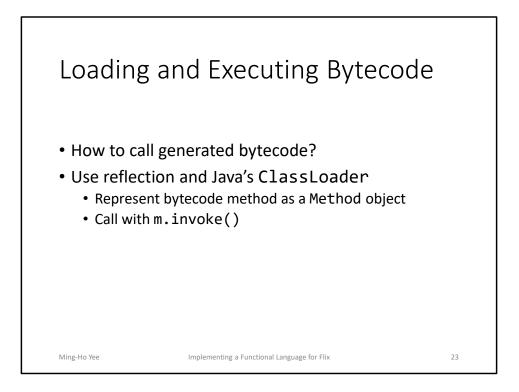
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- We convert all lambda functions into closures.
 - The closure contains an inner lambda function.
 - The original function is rewritten to pass the captured variables.
 - The closure contains the values that are captured.
- At closure creation, we save the values that need to be passed into the function.
- At closure call (ApplyClosure), the saved values ae combined with the closure arguments and passed to the implementing function.
 - Now we can safely lift the inner lambda, giving it a name.
- We'll get back to MkClosure and ApplyClosure later.



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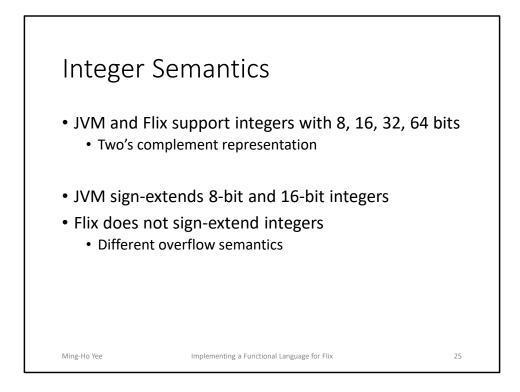
- Two back-ends for the functional language:
 - Interpreter original one, easy to understand and maintain, good for debugging and prototyping features.
 - Code generator now the default back-end, more complicated, but better for performance.
- Since Flix is implemented on the JVM, the code generator targets the JVM.
 - Also good for portability.
- JVM is a stack machine, unlike x86, ARM, MIPS
 - Makes some things nicer: no register allocation since all operands and intermediate values go onto the stack.
 - Makes some things harder: need to compute maximum stack height, manage constant pool, compute metadata for bytecode verifier.
 - Use the ASM library to handle these tasks.
 - Scala 2.12 uses ASM.
- There's a few interesting codegen problems to discuss today.



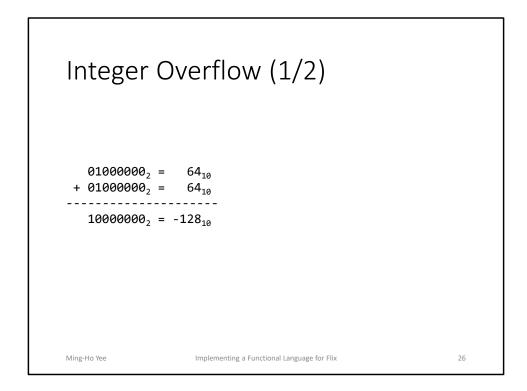
- ASM library produces bytecode as an array of bytes.
 - For convenience, we want to load it immediately, instead of writing to disk.
 - Then we need to be able to execute it.
- We use reflection and Java's ClassLoader.
 - Each bytecode method is represented by a reflection Method object.
 - Call a method with m.invoke().
- We store Method objects on the AST.
 - Each function has an expression AST and a Method object.

Flix Type	ЈVМ Туре	
	Primitive	Reference
Int8	byte	java.lang.Byte
Int16	short	java.lang.Short
Int32	int	java.lang.Integer
Str		java.lang.String
Тад		Value.Tag
Tuple		Value.Tuple

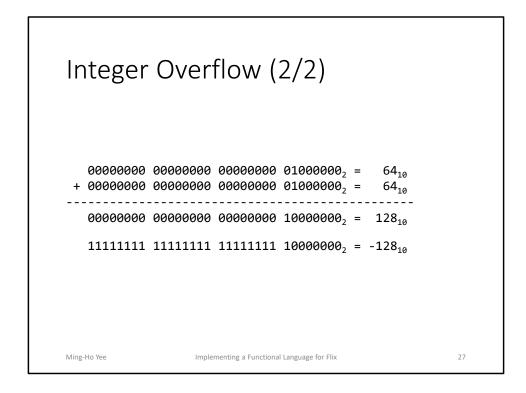
- Flix values are represented as primitives whenever possible.
 - E.g. Int32 -> int
 - Sometimes values need to be boxed, e.g. java.lang.Integer.
- Some Flix values are represented as Java reference types.
 - E.g. Str -> java.lang.String
- Other Flix values have no corresponding class in the Java standard library, so Flix defines them.
 - Tag -> Value.Tag
 - Tuple -> Value.Tuple
 - Tags and tuples are generic in the values they contain, so Flix has to use reference types and type erasure.
 - Box Int32 as a java.lang.Integer and then store as java.lang.Object.
 - When extracting the value, need to cast or unbox.
 - Code generator emits the code to do this automatically.



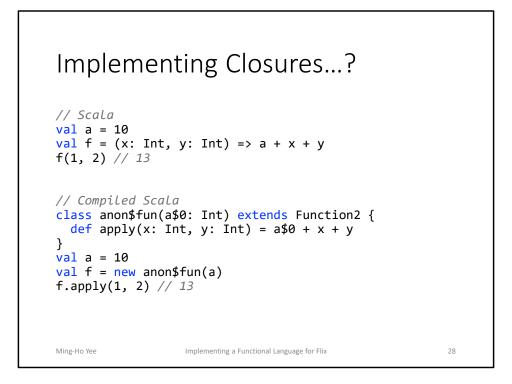
- Both the JVM and Flix support signed integers, with 8, 16, 32, and 64 bits.
 - Use two's complement representation.
- Implementation detail of the JVM: sign-extend 8-bit and 16-bit integers to 32 bits.
 - The JVM is designed for 32-bit integers and operations.
 - A "surprise" from compilers class: adding two 8-bit integers returns a 32-bit integer.
- Flix does not sign-extend integers.
 - This may be harder to implement, but conceptually, it's easier to understand.
 - Leads to some differences, specifically with overflow.
- The problem is to implement Flix semantics on the JVM, which has different semantics.



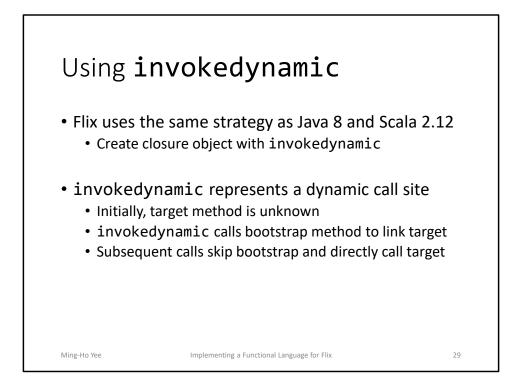
- Consider adding two 8-bit integers with value 64.
 - Mathematically, the result is 128.
- But this cannot be represented in two's complement with 8-bits.
 - The result we get is the 8-bit representation for -128.



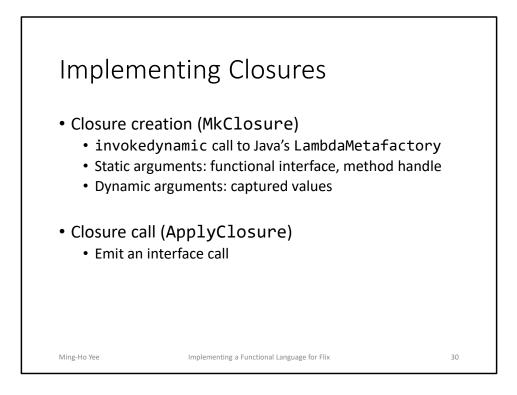
- On the JVM, the operands are sign-extended.
 - We get the 32-bit representation for the same value, 64.
- But the binary result now represents a different number, 128.
 - This is the correct mathematical result, but not the result according to Flix semantics.
- Fortunately, the JVM has a "truncate to 8 bits and sign-extend" instruction, I2B.
 - This gives us the 32-bit representation of -128, the desired result.
- This is something we have to do for integer expressions, including all arithmetic and some bitwise expressions.



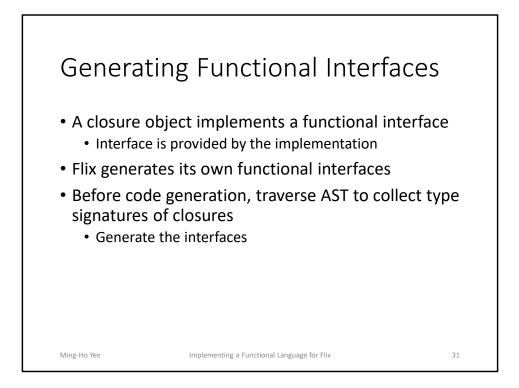
- In object-oriented languages, one way to implement closures is to use function objects.
 - C++, C#, and Scala 2.11 use this method.
- Every lambda function has an associated anonymous class.
 - The class stores captured variables, and defines a method that implements the lambda function.
- Creating a closure instantiates that class, with values of captured variables.
 - Here, a is passed to the constructor.
- Calling a closure is an interface call on the method.
- Problem with this approach: must generate an anonymous class for each lambda function. Increases code size.



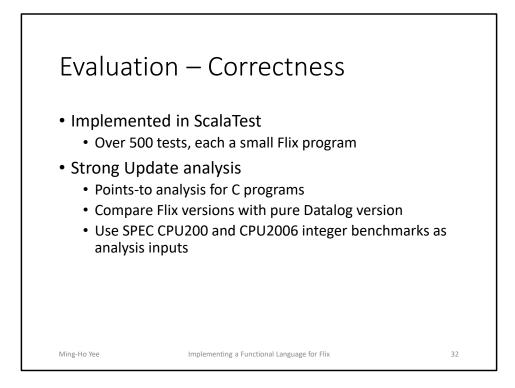
- An alternate approach, used by Java 8 and Scala 2.12, is invokedynamic.
 - Instead of the code generator statically creating the classes, invokedynamic will dynamically create the classes.
- Initially, the invokedynamic instruction is a dynamic call site, and the target of the call is unknown
 - To determine the target, invokedynamic calls a bootstrap method, and then links it
 - Subsequent calls bypass the bootstrap and directly call the target
 - In other words, let the run time determine which method is called, but then permanently link it so future calls are "static"



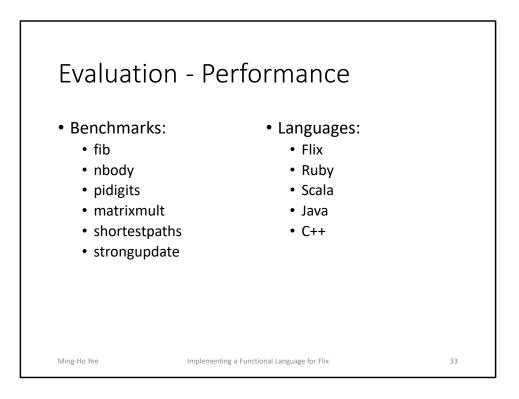
- To create a closure, code generator emits an invokedynamic call to LambdaMetafactory, which is defined in the Java standard library.
 - Static arguments represent the functional interface implemented by the closure, and a handle to the method implementing the function.
 - Dynamic arguments represent the captured values.
- When a closure is created for the first time, invokedynamic calls the metafactory, which generates an anonymous class.
 - The class is instantiated with the captured values.
- Subsequent calls bypass the metafactory and directly instantiate the class.
- Closure call
 - Emit an interface call.
 - The closure will automatically supply the captured values to the implementing function.



- Each closure object needs to implement a functional interface.
 - Functional interface: interface with a single abstract method.
 - The interfaces must be provided by the implementation.
 - Java provides a very small selection.
 - If you're writing lambdas in Java and can't find the interface you need, you have to define your own.
 - Scala is the opposite extreme.
 - Very general interfaces, all generic
- Flix generates its own functional interfaces.
 - Traverse the AST, find every lambda function, and generate an interface for each unique type.
 - Generates only the interfaces that are needed.
 - Interfaces are specialized, so no generics and no boxing/unboxing.



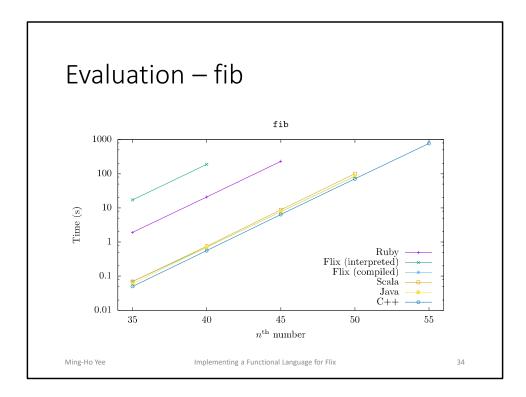
- 15:00 (38:00 total) to get here
- It's important to ensure the code generator produces the right code.
- Almost all of the tests are written in the ScalaTest framework.
 - Over 500 tests, each a small and complete Flix program.
- For a larger test, we use the Strong Update analysis, which is a real-world static analysis.
 - Exercises logic code as well as functional code.
 - A points-to analysis for C programs.
 - Achieves better precision by propagating singleton sets flowsensitively.
 - Does not sacrifice performance by propagating non-singleton sets flow-insensitively.
 - Compare the two Flix implementations to a Datalog reference implementation.
 - Datalog implementation must simulate lattices.
 - Run on the DLV solver.
 - Use SPEC integer benchmarks as analysis inputs.



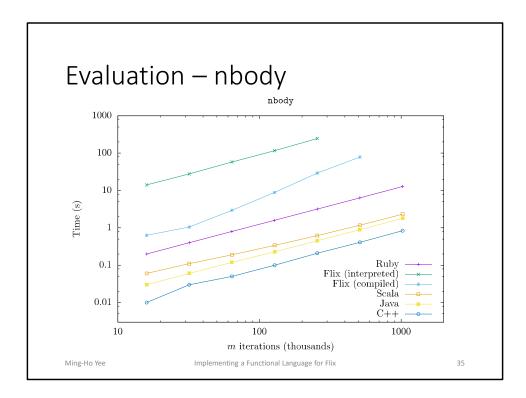
- Benchmarks:
 - Purely functional, so compared against implementations in other languages.
 - fib naïve implementation of Fibonacci, taking exponential time.
 - nbody Computer Languages Benchmarks Game; N-body simulation that models Sun and gas giants
 - pidigits CLBG; computes the digits of pi one at a time; requires arbitrary-precision arithmetic
 - Require the solver, so only compiler vs interpreter
 - matrixmult multiply two random matrices together, using cubictime algorithm
 - shortestpaths based on the Floyd-Warshall algorithm for all-pairs shortest paths
 - Real static analysis
 - strongupdate the Strong Update analysis; also compared with Datalog and handwritten C++ analyzer
- Languages
 - Flix both compiled and interpreted. Purely functional language, so data structures need to be copied and not mutated in place. No tail call

optimization.

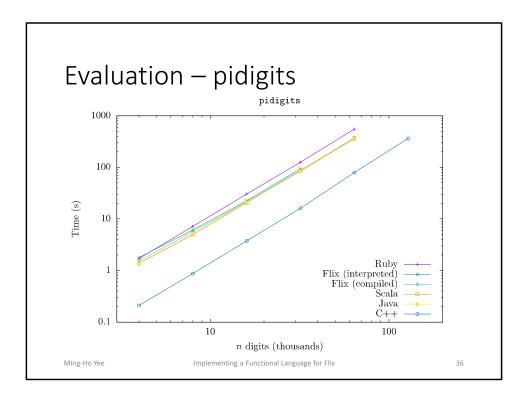
- Ruby dynamic language with a bytecode interpreter.
- Scala JVM language; benchmarks written in functional style.
- Java benchmarks written on OO-style.
- C++ benchmarks written in OO-stye.



- Compiled Flix is 250x faster than interpreted Flix
- Fibonacci is a simple function, so the compiled bytecode for Flix, Scala, and Java is very similar.
- Scala is slower than Flix
 - Scala convention put the methods in a singleton object, which get compiled to instance methods.
- Ruby is faster than Flix interpreter
 - Bytecode interpreter vs AST interpreter



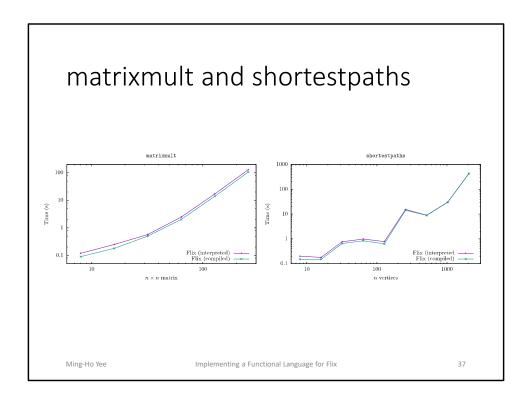
- Both Flix implementations are the slowest.
 - But compiled Flix is 17x faster than interpreted Flix.
- nbody is the most complicated functional program implemented in Flix, and highlights many inefficiencies.
 - No tail call optimization, so the stack memory usage increases until the stack overflows.
 - Interpreter needs to copy the environment for each call, which becomes expensive.
- C++ is the fastest
 - Compiler can emit vector instructions.



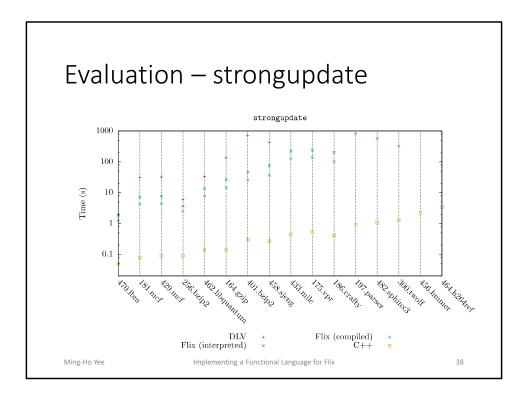
- Interestingly, Ruby, Flix, Scala, and Java are all very similar.
 - Though Ruby is a bit slower, and C++ is the fastest.
 - The bottleneck is in the arbitrary-precision arithmetic.

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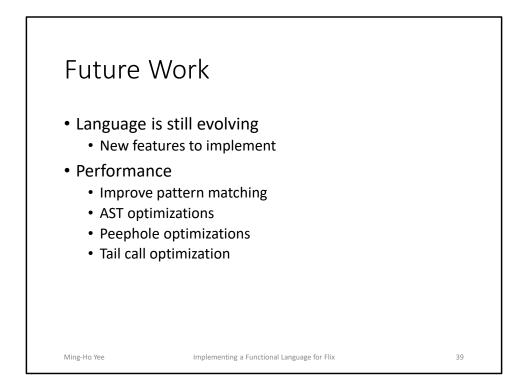
- Java, Scala, and Flix all use the same library (java.math.BigInteger).
- Doesn't matter if other parts of the program are slower.
- Ruby and C++ use the same C library: GNU Multiple Precision Arithmetic Library.
 - But Ruby is much slower, probably because of overhead as a dynamic language.
 - Calling + involves a lot of overhead before the call makes it to the C library.



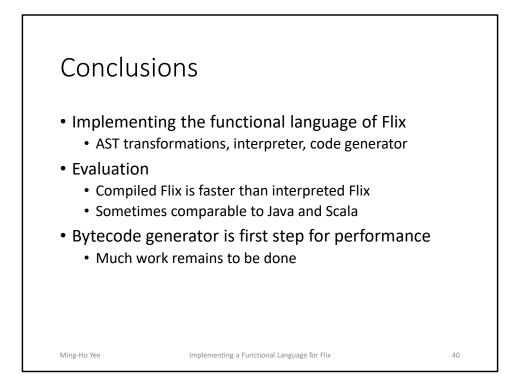
- matrixmult and shortestpaths is very expensive.
- Most of the time is spent in the solver, evaluating the logic code.
- Functional code has very little effect.
 - So very little difference between interpreter and code generator.



- Differences are consistent.
 - Datalog slower than interpreted Flix, slower than compiled Flix, slower than C++.
- The analysis requires a constant propagation lattice.
 - In Datalog, the lattice is simulated as a power set lattice, which is much more expensive.
 - In Flix, the lattice can be expressed directly.
 - So interpreted Flix is 3.7x faster than Datalog.
 - Compiled Flix is 1.7x faster than the interpreter.
- C++ is even faster, at 126x.
 - Flix is a general framework implemented in Scala, so already at a disadvantage compared to C++.
 - The C++ implementation also has a specific optimization to reduce memory usage.
 - Some elements of the lattice occur much more frequently.
 - The C++ analyzer uses a special data structure that can implicitly represent these elements.
 - But Flix must explicitly represent them.



- Two main areas for future work.
- New language features:
 - The language is still evolving.
 - Some features may be isolated to the logic code, or can be implemented in just the front-end.
 - Otherwise, features need to be implemented twice, in the interpreter and the code generator.
 - Interpreter should make it easier to prototype and test.
- Performance is the big category.
 - Hook calls could be more direct, rather than going through the Flix object and invoke method.
 - Pattern matching could be optimized.
 - AST optimizations: constant propagation, copy propagation, dead code elimination.
 - Peephole optimizations on the generated bytecode.
 - Tail call optimization, since we need recursion.
- And slightly unrelated: code generation for logic language.
 - This will probably have the most benefit, since the solver is a major bottleneck for performance.



- 5:00 (43:00 total) to get here.
- To summarize:
 - This thesis concerned the implementation of the Flix functional language.
 - First the interpreter, then the code generator, and also common AST transformations.
- Evaluation finds that the compiled code is faster than the interpreted code.
 - Especially for benchmarks that spend most of the time in functional code
 - In some cases, Flix is comparable to Java and Scala.
 - However, Flix is still slower than a handwritten C++ static analyzer.
- The bytecode generator is only the first step for performance.
 - There is much work remaining.